

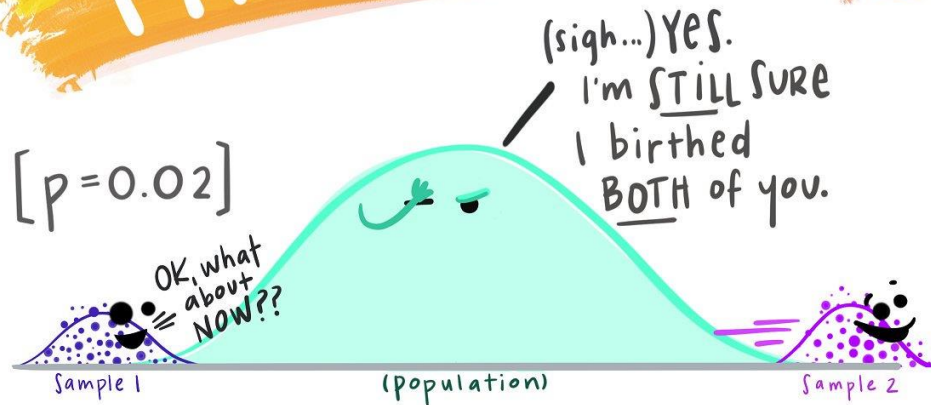
# Modelação Ecológica

## AULA I I

22 October 2019 – 14:00-16:30 – room 2.3.37

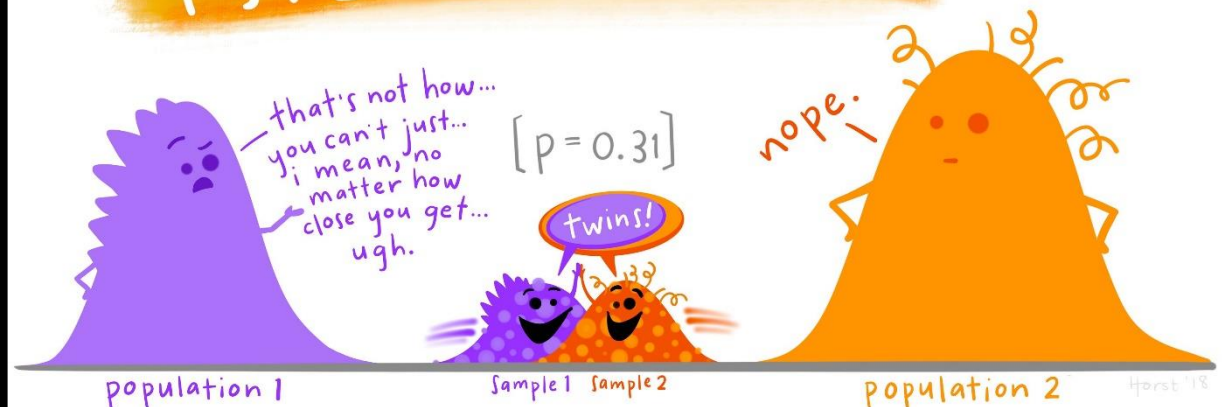
Tiago A. Marques

# TYPE 1 ERRORS

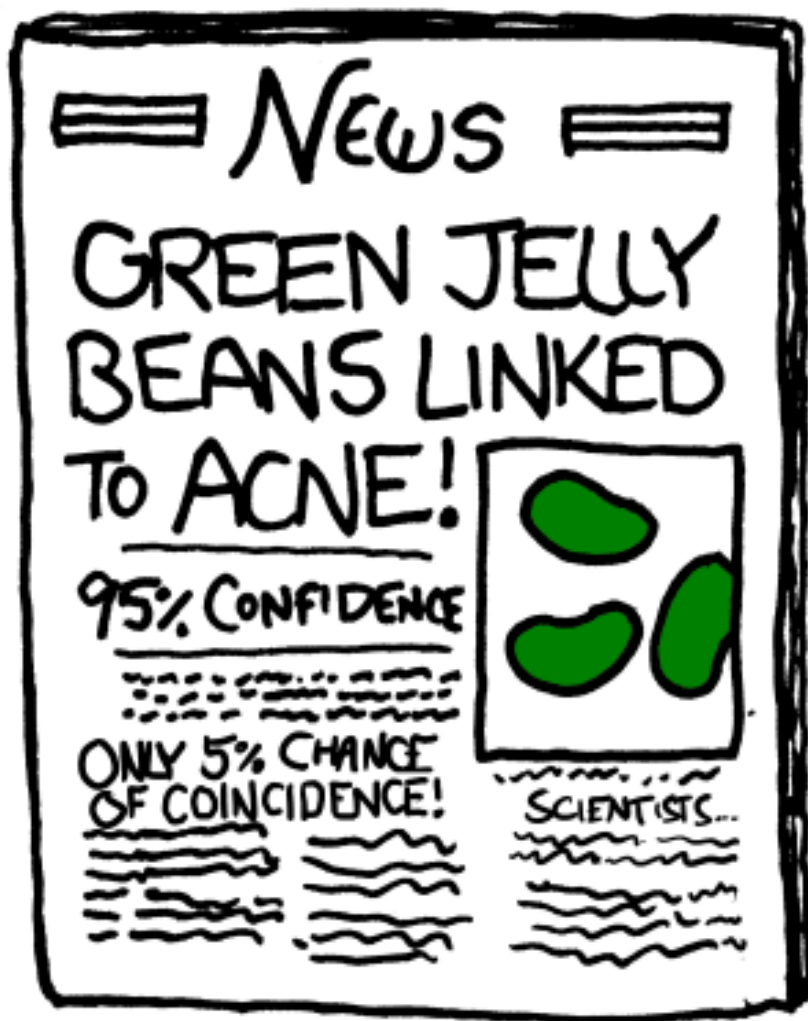


Horst '18

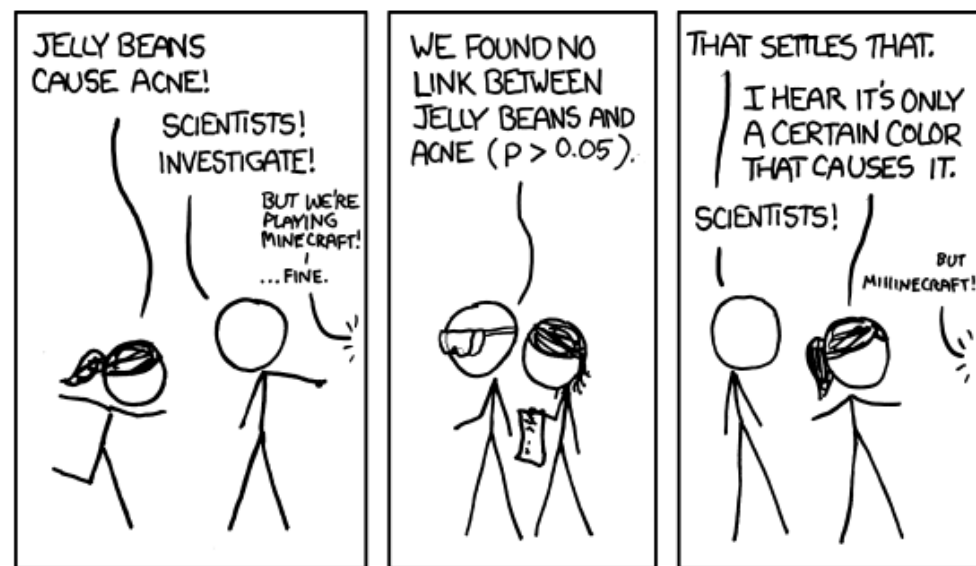
# TYPE II ERRORS:



Horst '18



<https://xkcd.com/882/>



Se não conhecem o xkcd.com... vale a pena explorar!

WE FOUND NO  
LINK BETWEEN  
PURPLE JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
BROWN JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
PINK JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
BLUE JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
TEAL JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
SALMON JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
RED JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
TURQUOISE JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
MAGENTA JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
YELLOW JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
GREY JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
TAN JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
CYAN JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND A  
LINK BETWEEN  
GREEN JELLY  
BEANS AND ACNE  
( $P < 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
MAUVE JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
BEIGE JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
LILAC JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
BLACK JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
PEACH JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



WE FOUND NO  
LINK BETWEEN  
ORANGE JELLY  
BEANS AND ACNE  
( $P > 0.05$ ).



## Publication bias: What are the challenges and can they be overcome?

Ridha Joobar, MD, PhD; Norbert Schmitz, PhD; Lawrence Annable, Dipstat;  
Patricia Boksa, PhD

Joobar, Boksa — Douglas Mental Health University Institute and Department of Psychiatry, McGill University, Montréal, Que.;  
Schmitz, Annable — Department of Psychiatry, McGill University Health Centre, Montréal, Que.

Appearances to the mind are of four kinds.  
Things either are what they appear to be;  
Or they neither are, nor appear to be;  
Or they are, and do not appear to be;  
Or they are not, and yet appear to be.  
Rightly to aim in all these cases  
Is the wise man's task.  
Epictetus, 2nd century AD

In the last few years, several meta-analyses<sup>1-4</sup> have reappraised the efficacy and safety of antidepressants and concluded that the therapeutic value of these drugs may have been significantly overestimated (see Ioannidis<sup>5</sup>). In some instances, the authors of these meta-analyses resorted to the United States' Freedom of Information Act to obtain unpublished data that, when included in meta-analyses with previously published data, reduced significantly the purported

that they are more likely to be considered for publication by editors, more favourably reviewed by peers and, once published, more likely to be cited. For editors, it is the competition for citation index and the financial survival of journals that makes it more attractive to publish positive findings.

Although publication bias has been documented in the literature for decades and its origins and consequences debated extensively, there is evidence suggesting that this bias is increasing. A recent investigation covering more than 4600 publications from different countries and disciplines found strong evidence for a steady and significant increase in publication bias over the years. The frequency of papers declaring significant statistical support for their a priori formulated hypotheses increased by 22% between 1990 and 2007 ( $n = 4656$ ,  $p < 0.001$ ). Psychology and psychiatry are among the disciplines in which this increase is highest ( $p < 0.001$ ).<sup>7</sup> A

# Gestão de Páginas

- ▼ Modelação Ecológica
  - Modelação Ecológica(Ecologia Marinha)
  - Modelação Ecológica(Ecologia e Gestão Ambiental)
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  - ▶ Aula1
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    - GLM example
    - Parques Eólicos
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  - ▶ PDFs
  - ▶ R Cheat Sheets
  - ▶ Propostas de resolução de fichas de trabalho
- ▶ Avaliação

+ Criar

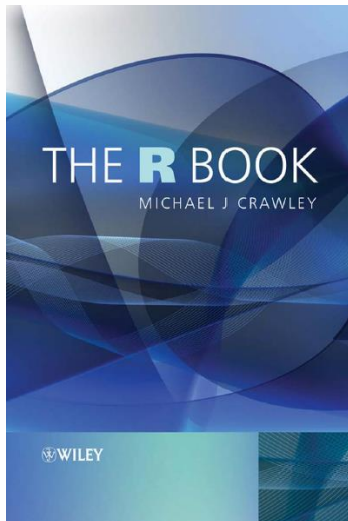
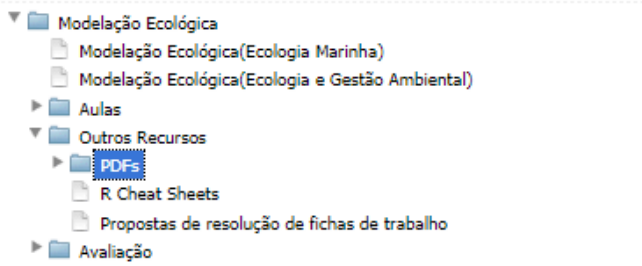
## PDFs

Página   Ficheiros 11   Permissões   Link

Adicionar Ficheiro

#	Nome
1	Modelling ecological systems in a changing world <i>Evans2012.pdf</i>
2	Norberg_et_al-2019 A comprehensive evaluation of predictive performance of 33 species distribution models at species and community levels <i>Norberg_et_al-2019-Ecological_Monographs.pdf</i>
3	The importance of stupidity in scientific research <i>Schwartz2008.pdf</i>
4	Ecological Models and Data in R <i>Bolker2007.pdf</i>
5	Numerical Ecology with R <i>Borcardetal2001EcologyUseR.pdf</i>
6	Introduction to Probability and Statistics Using R <i>IPSUR.pdf</i>
7	A Beginner's Guide to R <i>Zuuretal2009useR.pdf</i>
8	Analyzing Ecological Data <i>zuur_2007.pdf</i>
9	Mixed Effects Models And Extensions In Ecology With R <i>Zuur_Mixed-effects-models-and-extensions-in-ecology-with-R.pdf</i>
10	The R Book.pdf
11	Publication bias: What are the challenges and can they be overcome? <i>jpn-37-149.pdf</i>

# NEW RESOURCE: THE R BOOK



## PDFs

Página

Ficheiros 10

Permissões

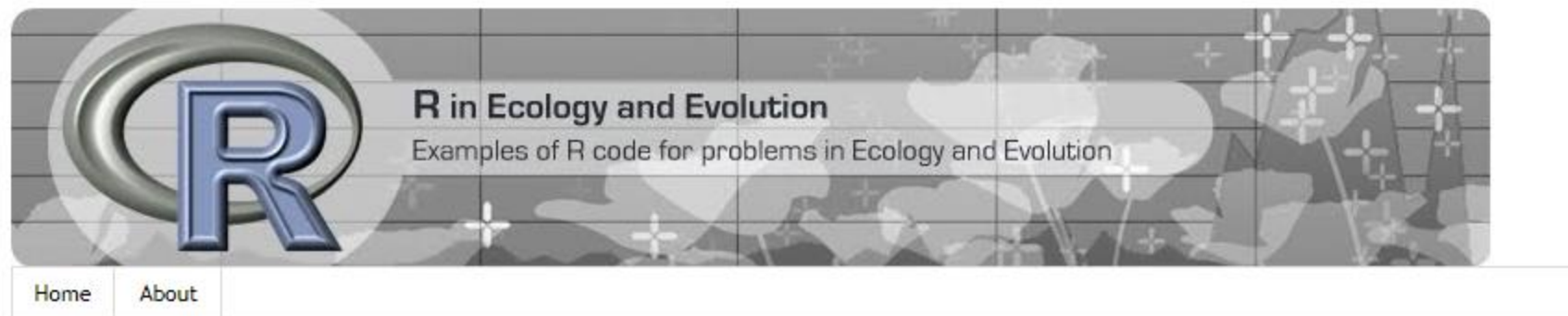
Link

Adicionar Ficheiro

#	Nome
1	Modelling ecological systems in a changing world <i>Evans2012.pdf</i>
2	Norberg_et_al-2019 A comprehensive evaluation of predictive performance of 33 species distribution models at species and community levels <i>Norberg_et_al-2019-Ecological_Monographs.pdf</i>
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10	The R Book.pdf



# Generalized Linear Models (continued!)



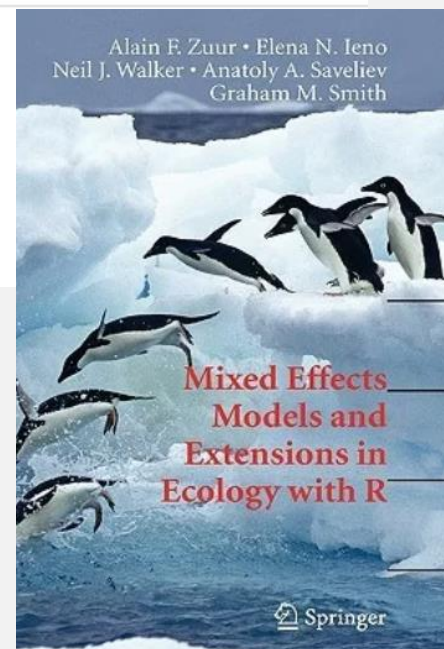
Sunday, May 14, 2017

A gentle introduction to Generalized Linear Models in R

What are generalized linear models?

<http://r-eco-evo.blogspot.com/2017/05/generalized-linear-models.html>

<http://spatialecology.weebly.com/r-code--data/category/glm>

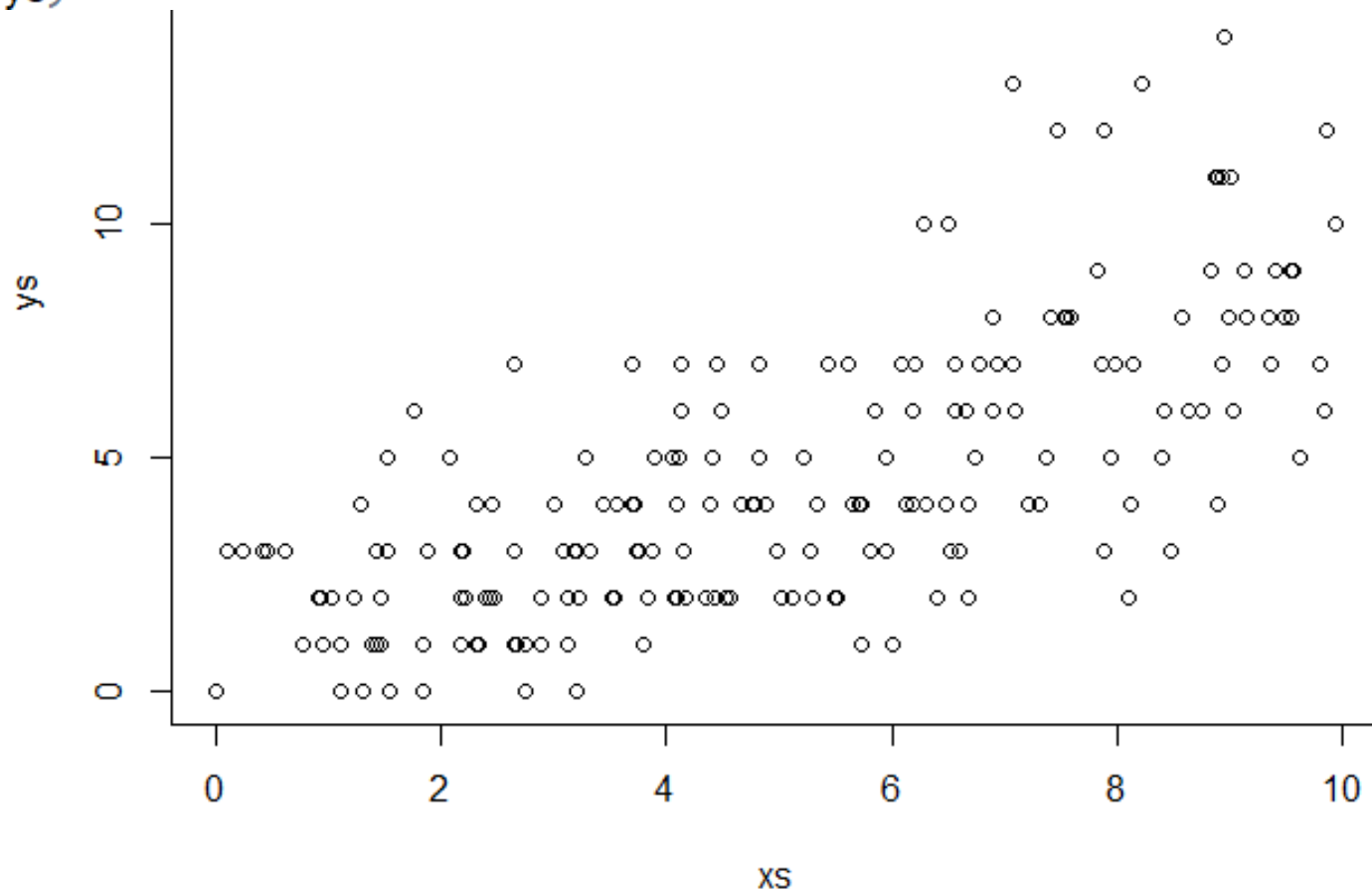




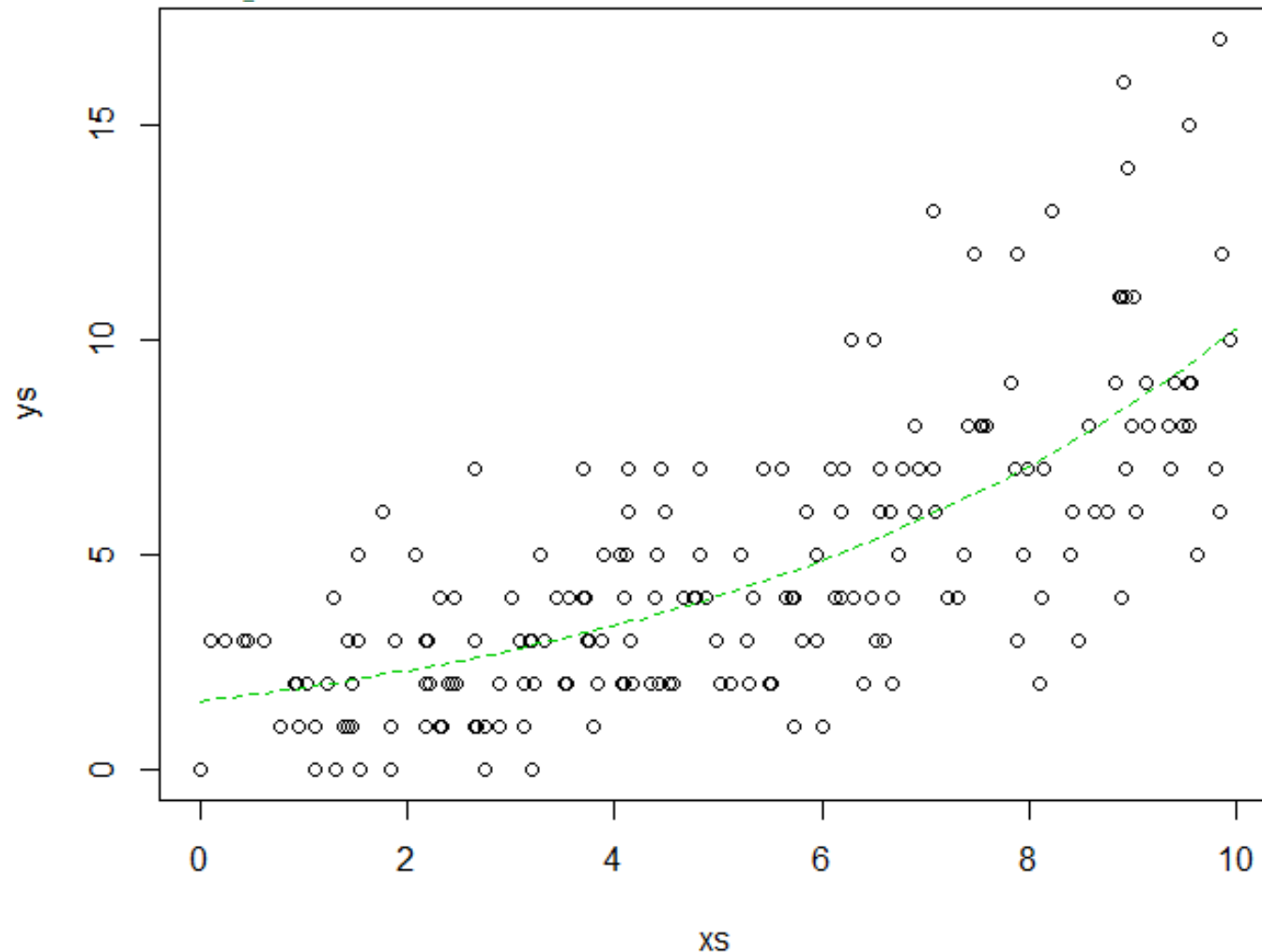
Working further  
on a GLM  
example

## Como ver o modelo GLM estimado?

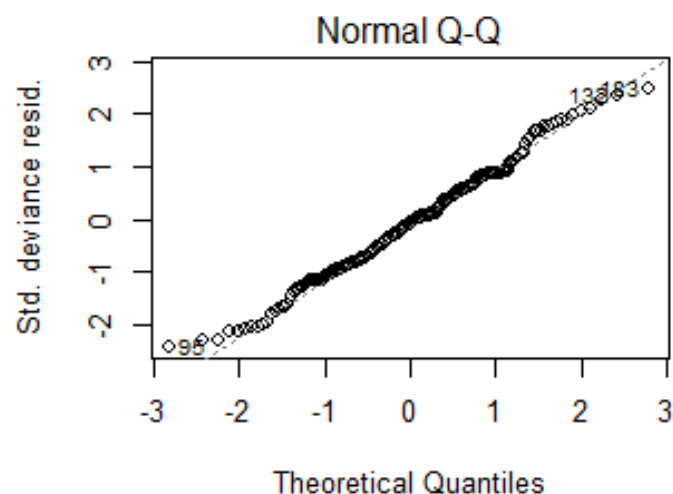
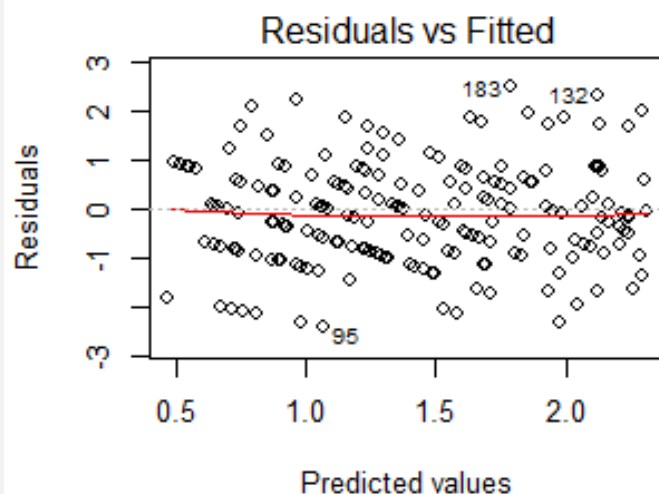
```
#creating data for a glm  
set.seed(123)  
#define the covariate  
xs=runif(200,0,10)  
#get the mean value  
Ey=exp(0.4+0.2*xs)  
#generate response  
ys=rpois(200,lambda=Ey)  
#plot data  
par(mfrow=c(1,1))  
plot(xs,ys)
```



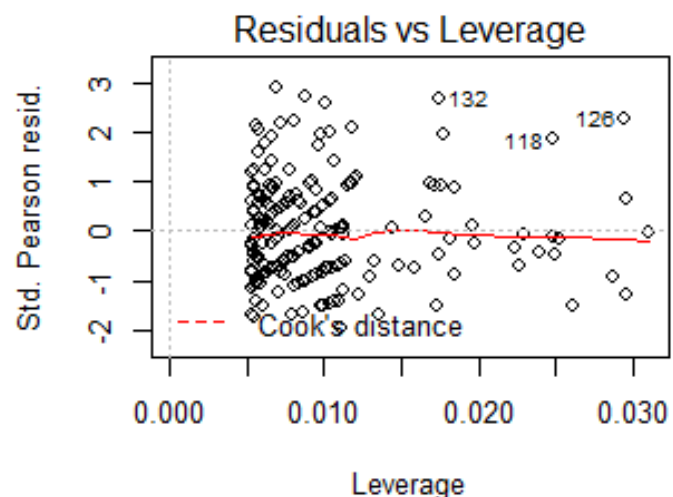
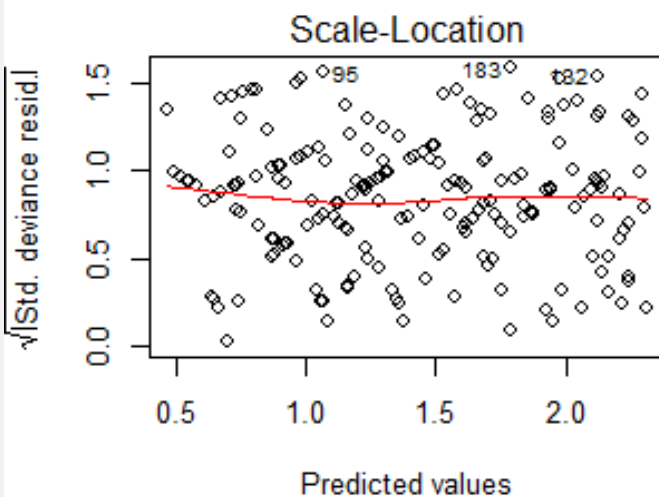
```
#fit model  
glm1=glm(ys~xs,family=poisson(link=log))  
#get new data for prediction  
newxs=seq(0,10,by=0.1)  
#predict  
predglm1=predict(glm1,newdata=data.frame(xs=newxs),type="response")  
#add fitted model  
plot(xs,ys)  
lines(newxs,predglm1,lty=2,col=3)
```



```
#diagnostics plot
par(mfrow=c(2,2))
plot(glm1)
```

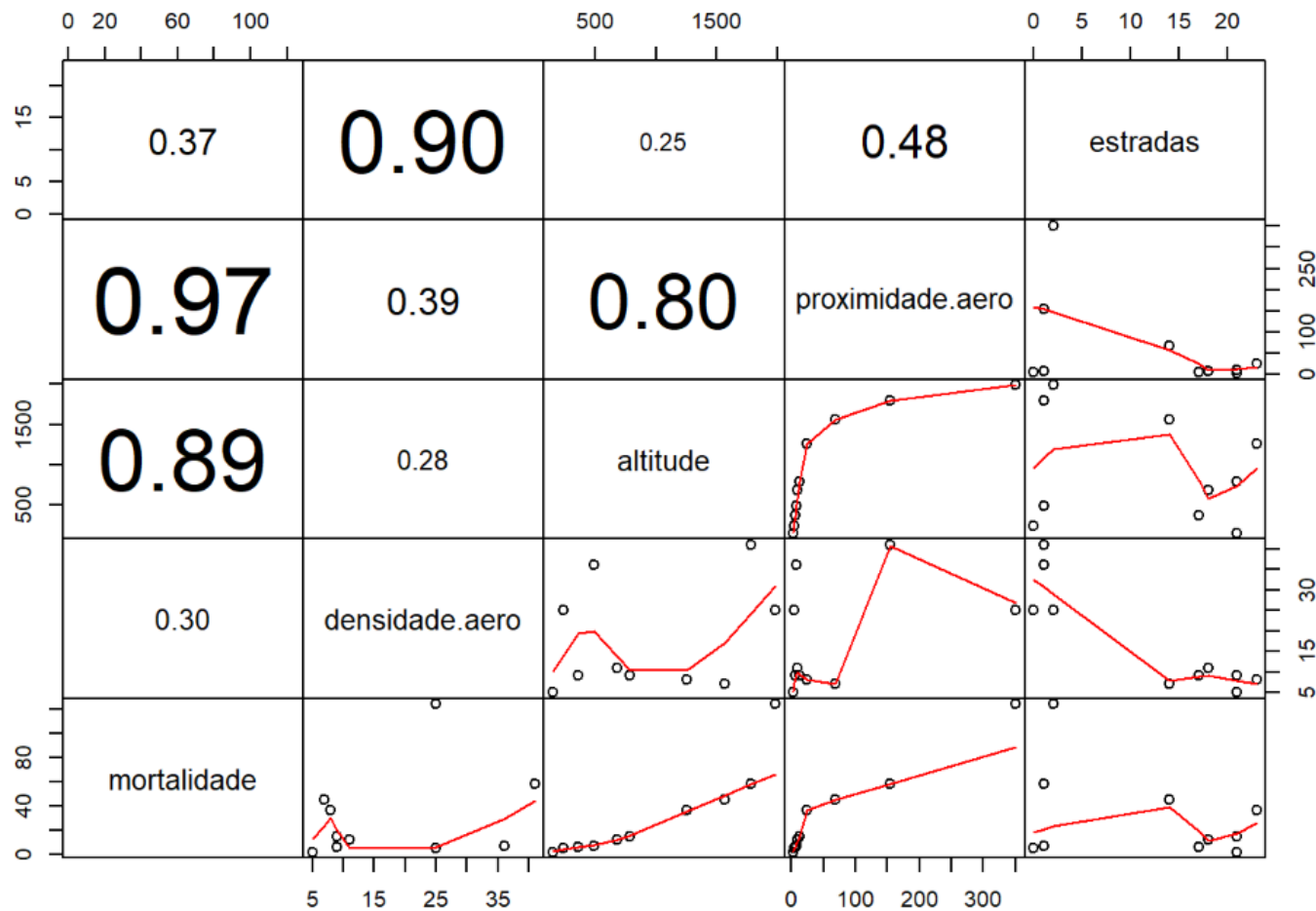


Note that now, even for residuals that are truly from a Poisson model, you get patterns in the residuals!



# HANDS-ON GLM

Usando os dados “parqueseolicos.csv”, pasta FENIX “Parques Eólicos” - Explicar a mortalidade em função de 4 variáveis independentes





```
regmul<-lm(mortalidade~., data=peol)
summary(regmul)
```

```
##
## Call:
## lm(formula = mortalidade ~ ., data = peol)
##
## Residuals:
##      1      2      3      4      5      6      7      8      9     10
## -2.146  1.872 -2.155  3.056 -1.753 -1.536  7.734 -2.491 -4.593  2.010
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    7.418208   10.009923   0.741 0.491957
## densidade.aero -0.394911    0.303776  -1.300 0.250299
## altitude        0.018310    0.004458   4.108 0.009286 **
## proximidade.aero 0.252193    0.029437   8.567 0.000357 ***
## estradas       -0.228630    0.446504  -0.512 0.630427
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.872 on 5 degrees of freedom
## Multiple R-squared:  0.9908, Adjusted R-squared:  0.9835
## F-statistic: 135 on 4 and 5 DF, p-value: 2.804e-05
```

```
library(MASS)
```

```
full.model<-lm(mortalidade~.,data=peol)
```

```
best.model<-stepAIC(full.model, direction="backward")
```

```
## Start: AIC=34.74
```

```
## mortalidade ~ densidade.aero + altitude + proximidade.aero +  
##      estradas
```

```
##
```

```
##           Df Sum of Sq    RSS    AIC
```

```
## - estradas      1         6.22 124.90 33.249
```

```
## <none>                118.68 34.738
```

```
## - densidade.aero  1        40.11 158.79 35.650
```

```
## - altitude       1       400.47 519.15 47.496
```

```
## - proximidade.aero 1      1742.14 1860.81 60.262
```

```
##
```

```
## Step: AIC=33.25
```

```
## mortalidade ~ densidade.aero + altitude + proximidade.aero
```

```
##
```

```
##           Df Sum of Sq    RSS    AIC
```

```
## <none>                124.90 33.249
```

```
## - densidade.aero  1        85.32 210.22 36.456
```

```
## - altitude       1       435.26 560.16 46.256
```

```
## - proximidade.aero 1      2465.64 2590.54 61.570
```

```
summary(best.model)
```

```
##
## Call:
## lm(formula = mortalidade ~ densidade.aero + altitude + proximidade.aero,
##     data = peol)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -5.248 -2.228 -1.510  2.738  7.114
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    2.665547   3.510035   0.759   0.4764
## densidade.aero -0.255509   0.126211  -2.024   0.0893 .
## altitude       0.017361   0.003797   4.573   0.0038 **
## proximidade.aero 0.259738   0.023866  10.883 3.57e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.563 on 6 degrees of freedom
## Multiple R-squared:  0.9903, Adjusted R-squared:  0.9855
## F-statistic: 205.1 on 3 and 6 DF,  p-value: 1.963e-06
```

With such a small number of variables, we might just fit all the models and pick the best!

This can be done using function `bestglm` in package `bestglm` (note that while the model is a simple linear model, the function can cope with GLMs too!).

The first argument **MUST** be a matrix with all the variables, and the last column needs to be the response variable.

```
library(bestglm)
bestGLM=bestglm(Xy=peol[,c(2:5,1)],family = gaussian,IC="AIC",RequireFullEnumerationQ=TRUE)
```

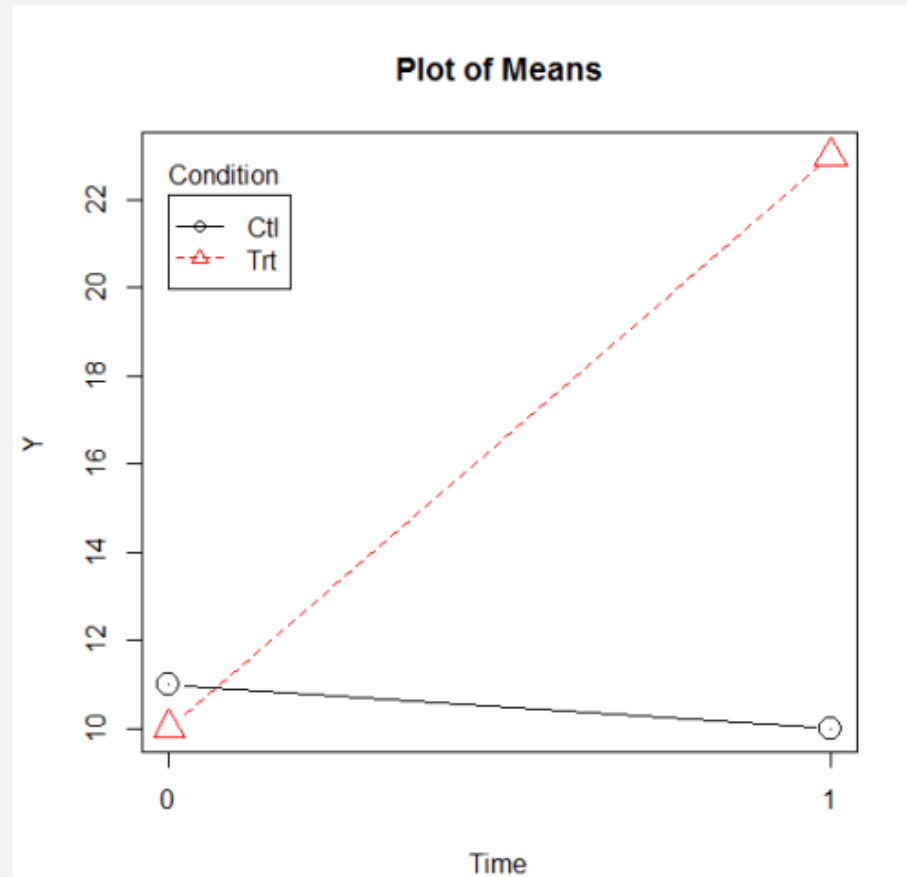
```
## Morgan-Tatar search RequireFullEnumerationQ=TRUE
```

```
bestGLM$BestModel
```

```
##
## Call:
## lm(formula = y ~ ., data = data.frame(Xy[, c(bestset[-1], FALSE),
##     drop = FALSE], y = y))
##
## Coefficients:
##      (Intercept)      densidade.aero      altitude  proximidade.aero
##           2.66555           -0.25551           0.01736           0.25974
```

In this case, we get the same result as the backwards procedure, which is reassuring, as for many variables, doing all the possible combinations becomes computationally intense.

# Regression with Interactions



<https://www.theanalysisfactor.com/interpret-main-effects-interaction/>

In a regression context we are usually interested in explaining a response variable as a function of independent covariates

$$\text{Response} = \text{function}(\text{var 1} + \text{var 2} + \dots + \text{var k})$$

The default approach is to consider that these independent covariates act independently on the response, but...

Sometimes the effect of one covariate might depend on the level of a factor or on the value of a second variable that one is considering – this is called an interaction

As an example, the impact on the weight of a fish of a given type of food might be dependent on the temperature at which the fish is living. In such a case we would say there is an interaction between temperature and diet in the determination of a fish weight.



When defining a model in R, we represent an interaction term between variables A and B as A:B. If we want to run a model to explain Y that includes variables A and B and their interaction, we can use

$Y \sim A + B + A:B$

or equivalently

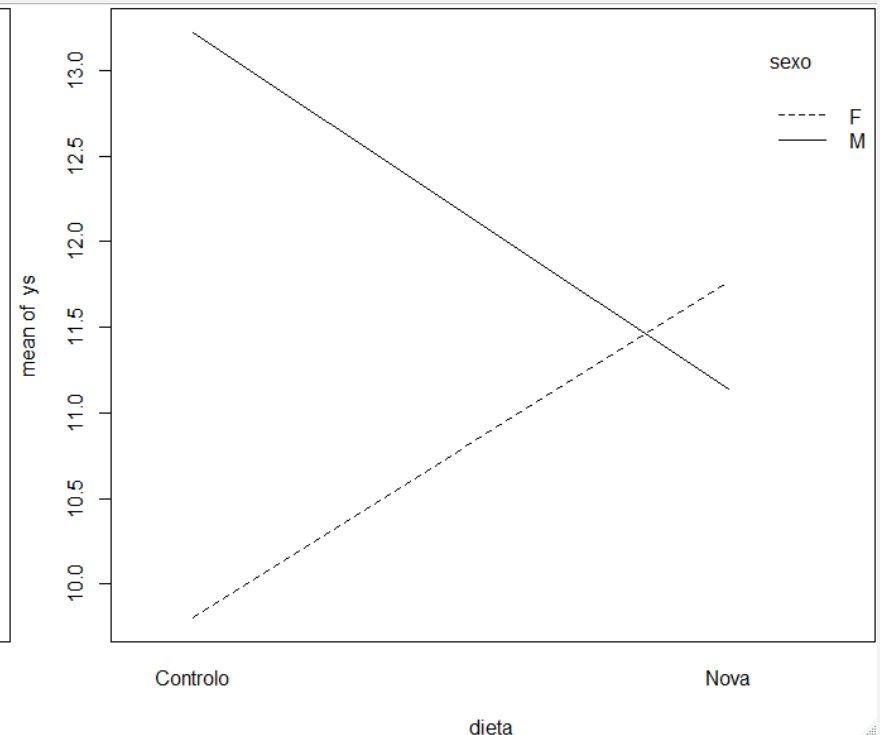
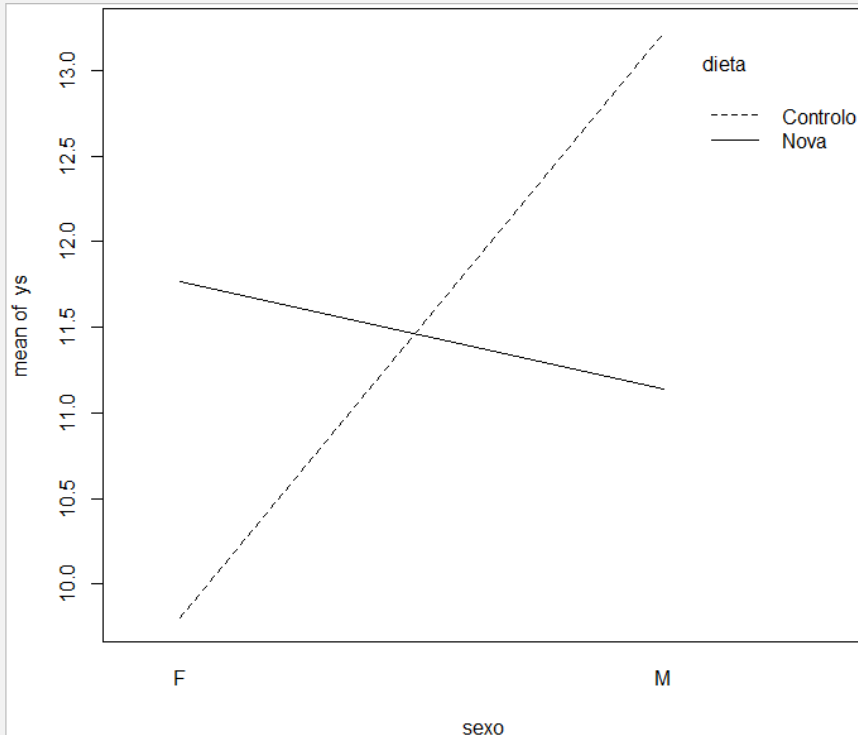
$Y \sim A * B$

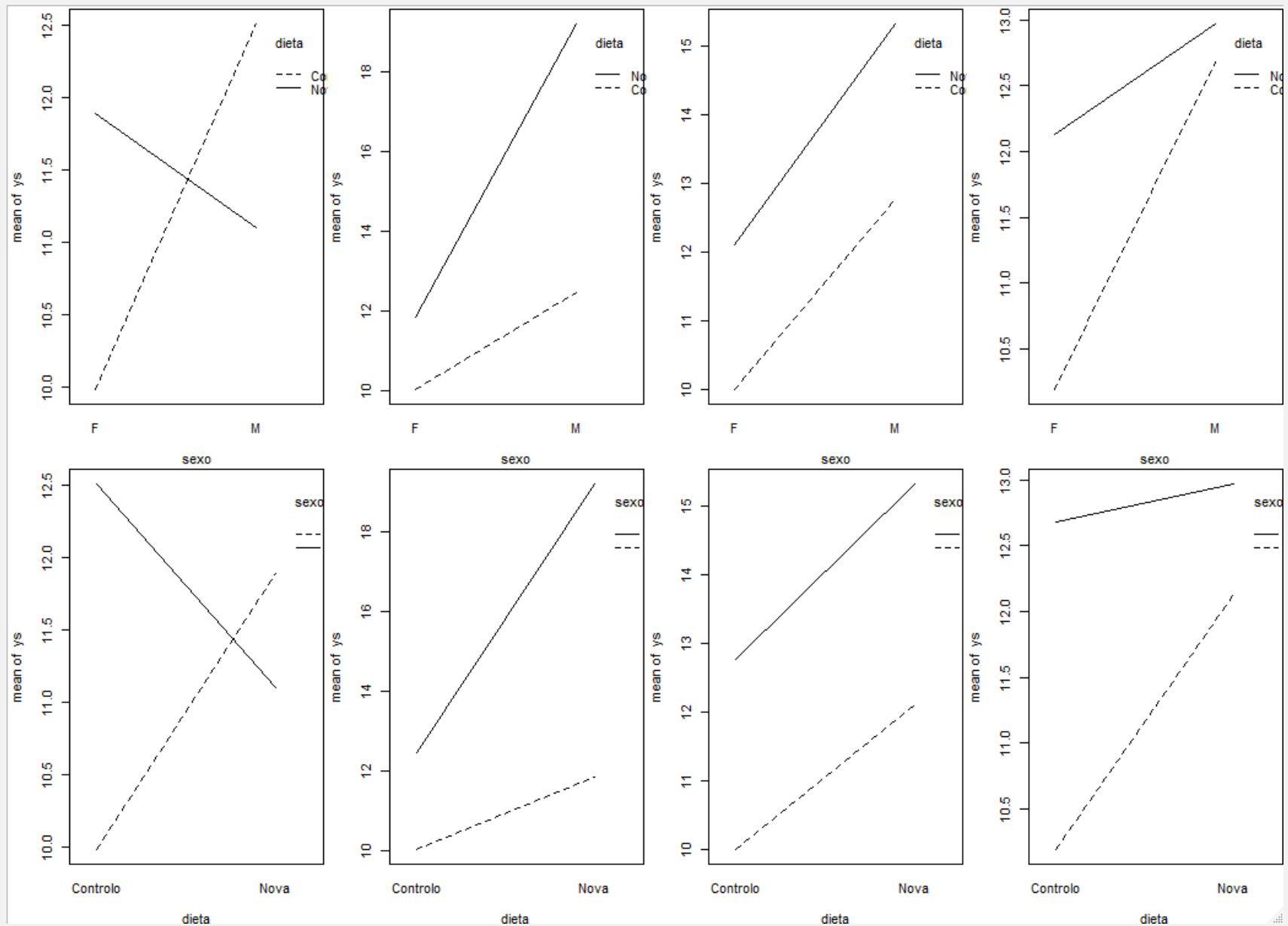
```
mod1=lm(ys~xs1+xs2+xs1:xs2)
mod2=lm(ys~xs1*xs2)
```

# What is really an interaction?

```
#-----  
#Interactions  
#### with factor covariates  
#-----  
set.seed(123)  
n=100  
sexo=rep(c("M","F"),each=n)  
dieta=rep(c("Controlo","Nova"),times=n)  
ys=10+3*(sexo=="M")+2*(dieta=="Nova")-4*(sexo=="M")*(dieta=="Nova")+rnorm(2*n,mean=0,sd=2)  
plot(ys~as.factor(paste0(sexo,dieta)))  
lmSDi=lm(ys~sexo*dieta)  
summary(lmSDi)  
  
par(mfrow=c(1,2),mar=c(4,4,0.2,0.2))  
interaction.plot(x.factor=sexo, trace.factor=dieta, response=ys)  
interaction.plot(x.factor=dieta, trace.factor=sexo, response=ys)
```

The new diet helps females gain weight, but it actually makes males lighter! In other words, the new diet is not better or worse, it depends on the sex!





interaction

interaction

interaction

interaction



A POLAR BEAR STORY...





# 2015 Barents Sea Polar Bear Survey



A photo selection by Tiago A. Marques































© Karen Lone 2015

# Interactions for continuous covariates

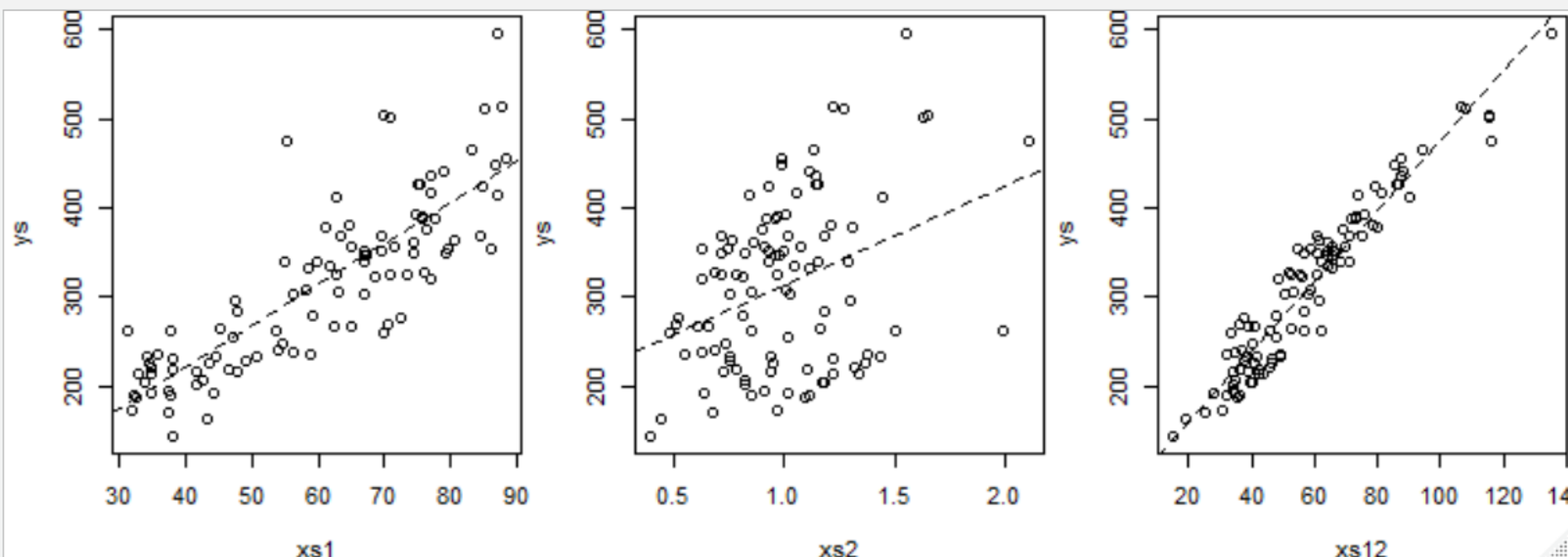
Aside: in fact, we already saw an example of an interaction when we were looking at a particular case of a regression model, the ANCOVA example, in the case of the ANCOVA with different slopes – that is an interaction effect, in which the slope of a relationship – i.e. the effect of one continuous covariate - depends on the level of a factor.

Now we can make it even more general if two or more quantitative covariates influence the response, but that response is dependent of the value of another covariate...

```
#sample size
set.seed(121)
n=100
#get a response variable
xs1=runif(n,30,90)
#get a second variable
xs2=rgamma(n,10,10)
#define the linear predictor
ys=20+2*xs1-4*xs2+3*xs1*xs2+rnorm(n,2)

#to make it easier
xs12=xs1*xs2
```

```
#plotting the data and partial models
par(mfrow=c(1,3),mar=c(4,4,0.2,0.2))
plot(xs1,ys)
abline(lm(ys~xs1),lty=2)
plot(xs2,ys)
abline(lm(ys~xs2),lty=2)
plot(xs12,ys)
abline(lm(ys~xs12),lty=2)
```



We can see that each of the variables per se,  $xs1$ ,  $xs2$  or their product  $xs12$  (i.e. their interaction) could be relevant to explain the response variable! But... hey...  $xs2$  seems to have a **positive** effect in the response!!!

The model implemented

Note these are estimates of true values of 20, 2, -4, 3

```
> summary(m1)
```

```
Call:  
lm(formula = ys ~ xs1 + xs2 + xs1:xs2)
```

Residuals:

Min	1Q	Median	3Q	Max
-2.7590	-0.6134	0.1005	0.6850	2.5857

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	23.21760	1.22479	18.956	< 2e-16 ***
xs1	1.97682	0.02030	97.368	< 2e-16 ***
xs2	-5.06833	1.09787	-4.617	1.21e-05 ***
xs1:xs2	3.01992	0.01876	160.986	< 2e-16 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.9462 on 96 degrees of freedom

Multiple R-squared: 0.9999, Adjusted R-squared: 0.9999

F-statistic: 3.272e+05 on 3 and 96 DF, p-value: < 2.2e-16

All terms are (not surprisingly given the plots) statistically significant!

Parameter standard errors: these depend on sample size and the true variability

Very high correlation – would probably never happen in practice!

Naturally the same happens with the overall test over the significance of regression models



```

#-----
#models with interaction
#model with interaction
m1=lm(ys~xs1+xs2+xs1:xs2)
#just the interaction term
m1B=lm(ys~xs1:xs2)
#same as m1
m1C=lm(ys~xs1*xs2)
#same as just the interaction term
m1D=lm(ys~xs12)
#-----
#models without the interaction term
mxs1xs2=lm(ys~xs1+xs2)
mxs1=lm(ys~xs1)
mxs2=lm(ys~xs2)

```

```
> AIC(m1,mxs1,mxs2,mxs1xs2)
```

	df	AIC
m1	5	278.6349
mxs1	3	1076.8927
mxs2	3	1183.9971
mxs1xs2	4	836.8333

```
> summary(mxs2)
```

```
Call:
lm(formula = ys ~ xs2)
```

```
Residuals:
```

Min	1Q	Median	3Q	Max
-161.03	-80.04	11.24	63.49	221.62

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	201.58	30.27	6.659	1.61e-09 ***
xs2	111.57	29.18	3.824	0.000231 ***

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 88.34 on 98 degrees of freedom
Multiple R-squared:  0.1299,    Adjusted R-squared:  0.121
F-statistic: 14.62 on 1 and 98 DF,  p-value: 0.0002307
```

Significant **positive** effect on  
the response...

```
> summary(mxslxs2)
```

```
Call:
```

```
lm(formula = ys ~ xs1 + xs2)
```

```
Residuals:
```

Min	1Q	Median	3Q	Max
-67.854	-6.369	0.761	7.561	52.010

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-156.08567	8.34374	-18.71	<2e-16 ***
xs1	5.11738	0.09208	55.57	<2e-16 ***
xs2	164.10708	5.20386	31.54	<2e-16 ***

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 15.49 on 97 degrees of freedom
```

```
Multiple R-squared:  0.9735,    Adjusted R-squared:  0.973
```

```
F-statistic: 1782 on 2 and 97 DF,  p-value: < 2.2e-16
```

Significant **positive** effect on  
the response...

Failing to include significant interactions could lead one to **wrongly** conclude that a variable that **in reality has a negative effect** on the response happens to have a significant **positive** impact on the response!

Therefore, exploring important interactions is important, and failing to include relevant ones might cause errors (while including spurious ones might also mask some real effects, see next slides!).

This was a 2-way interaction.

**One can** think about 3-way interactions or even higher order interactions, but **no one can** interpret those models anymore!

$$\text{modK} = \text{lm}(y \sim x_1 * x_2 * x_3 * x_4)$$

```

#-----
# A 4 way interaction model
#but in reality there is only 1 second order interaction
#-----
set.seed(123)
#get a response variable
xs1=runif(n,30,90)
#get a second variable
xs2=rgamma(n,10,10)
#get a response variable
xs3=runif(n,3,6)
#get a second variable
xs4=rgamma(n,4,4)
#define the linear predictor
ys=20+2*xs1-4*xs2+3*xs1*xs2+xs3+xs4+rnorm(n,2)
modK=lm(ys~xs1*xs2*xs3*xs4)
modL=lm(ys~xs1+xs2+xs3+xs4+xs1:xs2)
summary(modK)
summary(modL)

```

```
> summary(modK)
```

```
Call:
```

```
lm(formula = ys ~ xs1 * xs2 * xs3 * xs4)
```

```
Residuals:
```

Min	1Q	Median	3Q	Max
-2.5364	-0.6935	0.0393	0.6770	3.2611

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	17.15188	7.52582	2.279	0.0233	*
xs1	2.06364	0.11697	17.643	<2e-16	***
xs2	-0.76162	7.13759	-0.107	0.9151	
xs3	2.44263	1.70557	1.432	0.1530	
xs4	5.43081	7.56823	0.718	0.4735	
xs1:xs2	2.96404	0.11227	26.401	<2e-16	***
xs1:xs3	-0.02019	0.02628	-0.768	0.4429	
xs2:xs3	-1.06330	1.62602	-0.654	0.5136	
xs1:xs4	-0.04437	0.11307	-0.392	0.6950	
xs2:xs4	-3.36009	7.25366	-0.463	0.6435	
xs3:xs4	-1.36135	1.77582	-0.767	0.4438	
xs1:xs2:xs3	0.01356	0.02542	0.533	0.5941	
xs1:xs2:xs4	0.02494	0.10797	0.231	0.8175	
xs1:xs3:xs4	0.01629	0.02604	0.625	0.5321	
xs2:xs3:xs4	1.08330	1.71369	0.632	0.5277	
xs1:xs2:xs3:xs4	-0.01102	0.02513	-0.438	0.6613	

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 0.9978 on 349 degrees of freedom
```

```
Multiple R-squared:  0.9999,    Adjusted R-squared:  0.9999
```

```
F-statistic: 2.422e+05 on 15 and 349 DF,  p-value: < 2.2e-16
```

Type II  
errors

Including interactions which are not real can mask the true influence of relevant variables!!

```
> summary(modL)
```

```
Call:
```

```
lm(formula = ys ~ xs1 + xs2 + xs3 + xs4 + xs1:xs2)
```

```
Residuals:
```

	Min	1Q	Median	3Q	Max
	-2.77396	-0.67394	0.02921	0.72956	3.10716

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	21.899114	0.697442	31.399	< 2e-16	***
xs1	2.000077	0.010031	199.380	< 2e-16	***
xs2	-4.188672	0.616725	-6.792	4.61e-11	***
xs3	1.024842	0.059860	17.121	< 2e-16	***
xs4	1.105140	0.101134	10.927	< 2e-16	***
xs1:xs2	3.001929	0.009804	306.204	< 2e-16	***

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 0.9907 on 359 degrees of freedom
```

```
Multiple R-squared:  0.9999,    Adjusted R-squared:  0.9999
```

```
F-statistic: 7.372e+05 on 5 and 359 DF,  p-value: < 2.2e-16
```

```
> AIC(modL,modK)
```

	df	AIC
modL	7	1036.922
modK	17	1051.885